of substantial importance, such that exalted σ -values $(\sigma^+, \sigma^-, \text{ or both})$ are always required.

There is a strong suggestion, however, that *metu* and *pura* compounds do not fall on the same correlation lines. It is suggested that, in excited states, *meta* substituents enter into direct resonance interaction with a side chain and that consequently groundstate σ_m -values do not apply.

Acknowledgment.-The authors gratefully acknowledge the assistance of Messrs. John Gustafson and Myron DeLong, who have done much of the literature searching and data collecting which has been necessary. Helpful discussions with Mr. David L. Beveridge **are** gratefully acknowledged. Dr. John M. Vandenbelt of Parke, Davis and Company very kindly furnished us with substantial numbers of unpublished data, for which we are very grateful. All correlations were performed on an IBM 1620 computer at the University of Cincinnati Computing Center, supported by the **Ns**tional Science Foundation (Grant G19281).

The Application of the Hammett Equation to Amidines

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Ionization constants of C-substituted and of N-phenyl-C-substituted amidinium ions, of substituted guanidinium ions, and of 1-substituted 3-nitroguanidines were correlated with the Hammett equation using the σ_1 , σ_m , and σ_n constants. The amidinium sets gave best results with σ_m , the guanidinium and nitroguanidine sets with σ_I . Correlation of the ionization constants of substituted ammonium, methylammonium, dimethylammonium, and diethylammonium ions were made, best results being obtained with σ _I. The results indicate that in guanidinium ions and guanidines which bear electron-acceptor substituents, proton transfer involves the nitrogen atom bearing the substituent. The electrical effect in C-substituted amidinium ions is believed to be due to a short-range localized effect. The major component of the localized electrical effect in substituted ammonium ions appears to be the inductive rather than the field effect.

In the course of a previous investigation' we have studied the correlation of ionization constants of substituted carboxylic acids (I) with the Hammett equation.² As amides (II) are structural analogs of car-

$$
Q_{\rm X} = \rho \sigma_{\rm X} + Q_{\rm H} \tag{1}
$$

boxylic acids, and are in fact iselectronic with them, it seemed of interest to study the correlation of their ionization constants with the Hammett equation. No previous correlation of simple amidines with the Hammett equation is extant in the literature. Jaffé² has correlated data of Lorz and Baltzly³ on the ionization constants of **3-** or 4-substituted N,N-dibutylbenzamidines (III).

We have correlated ionization constants **(pKa** values), obtained from the literature, for C-substituted amidinium ions (IV), C-substituted N-phenylamidinium ions (V), and 1-substituted guanidinium ions (VI), and for 1-substituted 3-nitroguanidines (VII), with the Hammett equation using the σ_I , σ_m , and σ_p constants. The correlations were made as described by Jaffé.² The data used are given in Table I. The σ_m and σ_p constants used were taken from the compilation of Mc-Daniel and Brown,⁴ and the σ_1 constants used were from those given by Lewis and Taft, 5 whenever possible. Constants obtained from other sources are given in Table 11. The results of the correlations are presented in Table 111.

In some cases statistical factors were necessary to provide a common basis for correlation. **A** statistical factor of $\frac{2}{3}$ was used for $X = NH_2$ in the C-substituted amidinium set as in the following reaction (i) and

$$
[X-C(NH_2)_2]^+ + H_2O = X-C(NH)NH_2 + H_3O^+ \quad (i)
$$

guanidinium $(X = NH₂)$ is $\frac{3}{2}$ times as likely to react as are the other members of the series. When $X =$ PhNH in the C-substituted N-phenylamidinium set, a statistical factor of $\frac{1}{2}$ was used, as the ionizable proton is assumed to be that which is attached to the nitrogen bearing the phenyl group,^{6} and there are two such ionizable protons in this member of the set. When $X = H$ in the 1-substituted guanidinium ions, a statistical factor of $\frac{1}{6}$ was used since the ionizable proton in this set is assumed to be attached to the nitrogen atom bearing the strongest electron-acceptor substituent⁶; and when $X = H$ there are six equivalent protons. In the 3-nitro-1-substituted guanidines when $X = H$, a statistical factor of $\frac{1}{4}$ was used since there are four equivalent protons.

⁽¹⁾ M. Charton, Abstracts, **140th** National Meeting **of** the American Chemical Society, Chicago, Ill., Sept. **1961,** p. **91-Q.**

⁽²⁾ L. P. Hammett, "Physical Organic Chemistry," MoGraw-Hill **Book** Co., Inc., New York, N. Y., 1940; H. H. Jaffé, Chem. Rev., 53, 191 (1953); R. W. Taft, Jr., in "Steric Effects in Organic Chemistry," M. S. Newman, Ed., John Wiley and Sons, Inc.. New York, N. Y., **1956;** P. R. Wells, Chem. *Rev.,* **68, 171 (1963).**

⁽³⁾ R. Baltaly and E. Lora, *J.* Am. Chem. *SOC.,* **71, 3992 (1949).**

⁽⁴⁾ D. H. McDaniel and H. C. Brown, *J. Org. Chem.*, **23**, 420 (1958).

⁽⁵⁾ R. W. Taft, Jr., and **1.** C. Lewis, *J. Am.* Chem. *Soc., 80,* **2436 (1958). (6)** See discussion below.

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TABLE I Iours intox Coveniums Here tu Copper intour

^{*a*} At 20°. b At 24°. c Statistical factor of $^2/_3$ included. d A. Albert, R. Goldacre, J. Phillips, *J. Chem. Soc.*, 2240 (1948). e G.
Schwartzenbach and K. Lutz, *Helv. Chim. Acta*, 23, 1162 (1940). f Chem. Soc., 54, 1499 (1952). ^{*i*} W. M. Bruce, *ibid.*, 26, 449 (1904). ^{*m*} Includes statistical factor of $1/6$. ^{*n*} At 23°. *^o* Ref. 6; see also L. M. Hall, J. E. DeVries and E. S. Gantz, J. Am. Chem. Soc., 77, 6507 (1955). P. M. Yamashita and K. Sugino, J. Chem. Soc. Japan, 63, 1665 (1942). Chem. Soc. Japan, 63, 1665 (1942). Chem. Soc. Japan, W. Hoter, W. Heer, and M. Brenner, Helv. Chim. Acta, 44, 2154 (1961). ϵ P. F. Sommer and W. Simon, "Zusammenstellung von scheinbaren Dissoziation Konstanten im Losungsmittelsystem Methyl Cellosolve-Wasser," Vol. II, Ju

For comparison, we have also correlated the ionization constants of substituted ammonium, methylammonium, dimethylammonium, and diethylammonium ions. A statistical factor of 2 was used for symmetrical hydrazines owing to the presence of two equivalent basic sites. No statistical factor was used for 1.1-diethylhydrazine since Evans and Kynaston⁷ have shown on the basis of infrared spectra that protonation of 1,1-dimethyl- and 1,1-diisopropylhydrazine occurs at $N-1$.

(7) R. F. Evans and W. Kynaston, J. Chem. Soc., 3151 (1963).

TABLE I1 SUBSTITUENT CONSTANTS FROM SOURCES OTHER THAN

REF. 4 AND 5											
Substituent	σ _I	Ref.	σ_m	Ref.	σ_p	Ref.					
$_{\rm EtO}$	0.27	a									
$_{\rm PrO}$	0.27	\boldsymbol{a}									
BuO	0.27	a									
$CH_2=CHCH_2O$	0.33	Ъ	0.13	\boldsymbol{c}	-0.27	C					
$\rm Me_2N$	0.10	Ъ									
PhNH	0.02	α	-0.12	d	-0.40	d					
H ₂ NCO	0.27	\boldsymbol{a}			0.36	e					
\neg O2CCH2O	0.32	f	0.08	f	-0.39	f					
PhCH ₂			-0.01	h	-0.10	g					
$PhCH_2CH_2$	-0.01	a	-0.05	h	-0.14	i					
EtO ₂ CCH ₂	0.05	α	0.05	h	0.05	i					
NCH ₂	0.18	a	0.18	h	0.17	g					
i -Pr	-0.03	a	-0.07	h							
BzNH	0.29	\boldsymbol{a}									
i -Bu	-0.03	\boldsymbol{a}	-0.06	h							
$CH_2=CHCH_2$	0.00	\boldsymbol{a}	-0.04	h	-0.13	Ĵ					

^{*a*} M. Charton, *J. Org. Chem.*, **29,** 1222 (1964). ^{*b*} Estimated from the equation: $\sigma_1 = (3\sigma_m - \sigma_p)/2$: ref. 5. *^c* Calculated as described in M. Charton, *J. Org. Chem.*, **28,** 3121 (1963); from σ_m and σ_p for $\text{CH}_2=\text{CHCH}_2$ (see below). ^d Calculated as described in ref. c. $e \cdot \text{Ref. } c$. *f* A value for σ_{I} of CH_2CO_2 ⁻ was estimated from σ_1 , $c_{H_2}x = m\sigma_1 + c$; a value for σ_p - $c_{H_2}c_{O_2}$. from $\sigma_{p\text{-CH}_2X} = n\sigma_1 + d$ (M. Charton, unpublished result); from σ_p -cH₂x = $n\sigma_1$ + *d* (M. Charton, unpublished result);
a value for $\sigma_{m-\text{CH}_2\text{CO}_2}$ - from $\sigma_m = (2\sigma_1 - \sigma_p)/3$: ref. 5; σ_m and
 σ_p for OCH₂CO₂- were then calculated as in *d*; and σ_1 obtained
fr *Czech. Chem. Commun.*, **27,** 2296 (1962). h Estimated from $\sigma_m = (2\sigma_1 - \sigma_p)/3$: ref. 5. ^{*i*} Estimated from $\sigma_p \cdot \text{cf}_p x = n\sigma_1 + d$. ^{*j*} Estimated as in *i* from σ_p for CH₂=CH obtained from σ_p -xcH-cH $= p \sigma_{p-X} + q$ (M. Charton, dissertation, Stevens Institute of Technology, **1962).** ^aM. Charton, *J. Org. Chem.,* **29, 1222 (1964).**

Results

Amidinium Sets.—The results of the correlations in the two sets of amidinium ions clearly show that the with the results previously obtained with the substituted carboxylic acids.' σ_m constants give the best results. This is in accord

ionization of carboxylic acid and of amidinium ions is possible since the two reactions are not analogous. The reaction of amidines analogous to the ionization of carboxylic acids is

$$
X-C(NH)NH_2 + H_2O = [X-C(NH)_2]^- + H_3O^+ \quad (ii)
$$

whereas the reaction of carboxylic acids which is analogous to the ionization of amidinium ions is

$$
X-C(OH)2+ + H2O = X-CO2H + H3O+ (iii)
$$

It is interesting to note that the ratio of ρ for the amidinium ions (12.0) to ρ for the carboxylic acids $(8.03 \text{ in water at } 25^{\circ}, \text{ correlation with } \sigma_m^8)$ is 1.5, about the same as the ratio of ρ for substituted guanidinium ions to *p* for 1-substituted 3-nitroguanidines (see below), In both cases we are comparing charged to uncharged acids. This agreement may well be fortuitous. Apparently, the constant K-phenyl substituent in set *2* has little or no effect on the sensitivity of the reaction to substituent effects since the ρ -values for sets 1 and 2 are not significantly different.

Substituted Guanidinium **Ions** and 1-Substituted **3-** Nitroguanidines.-The substitute guanidinium ions give an excellent correlation with the σ_I constants, the results are significant at the 99.9% confidence level.

(8) M. Charton, unpublished results

RESULTS OF CORRELATIONS												
Set	σ	ρ	r^a	s^b	t^c	$Q_{\mathbf{H}}$	n^d					
1	I	-11.01	0.815	0.988	3.985	13 17	10					
	\boldsymbol{m}	-11.98	0.965	0.449	10.37	11.46						
	\boldsymbol{p}	-4.644	0.619	1.34	2.230	9.79						
$\boldsymbol{2}$	T	-14.63	0.931	0.742	4.402	11.29	5					
	\boldsymbol{m}	-12.08	0.999	0.0856	40.97	8.90						
	p	-6.372	0.877	0.974	3.159	6.69						
3	I	-24.09	0.990	0.801	17.05	14.20	8					
	$\scriptstyle m$	-17.70	0.908	2.36	5.295	11.83						
	\boldsymbol{p}	-7.800	0.648	4.29	2.083	8.47						
$\overline{\mathbf{4}}$	1	-16.44	0.980	0.401	10.99	12.33	7					
	\boldsymbol{m}	-8.282	0.779	1.26	2.780	10.89						
	\boldsymbol{p}	-2.833	0.559	1.67	1.507	10.15						
5	I	-20.64	0.979	0.682	14.31	9.59	11					
	\boldsymbol{m}	-21.12	0.881	1.57	5.587	8.12						
	\boldsymbol{p}	-20.44	0.131	3.29	0.397	7.51						
6	I	-12.64	0.994	0.155	21.19	9.11	7					
	\boldsymbol{m}	-8.788	0.555	1.23	1.493	8.24						
	\boldsymbol{p}	4.127	0.631	1.14	1.817	9.60						
7	I	-19.36	0.971	0.641	9.023	10.06	7					
	\boldsymbol{m}	-4.947	0.288	2.55	0.673	8.30						
	\boldsymbol{p}	8.013	0.652	2.02	1.923	10.30						
8	I	-18.77	0.965	0.891	10.38	9.16	10					
	\boldsymbol{m}	-14.62	0.717	2.36	2.910	7.45						
	\boldsymbol{p}	-0.402	0.036	3.39	0.101	6.91						
9	I	-20.21	0.973	0.959	9.465	9.89	7					
	\boldsymbol{m}	-17.93	0.856	2.16	3.697	8.52						
	\boldsymbol{p}	-6.053	0.464	3.70	1.170	7.31	1					

TABLE I11

^a Correlation coefficient. δ Standard deviation. ϵ Student t test. d Number of points in set.

The 1-substituted 3-nitroguanidines are also best correlated by the σ_I constants. Again the results are significant at the 99.9% confidence level. The ionization of the guanidinium ions is significantly more sensitive to substituent effects than is the ionization of 1 substituted 3-nitroguanidines, the ρ -values being 24.1 and 16.4, respectively.

Substituted Ammonium Ions.--Correlation of the stants have been reported by The results of Hall were unsatisfactory for our purpose, as correlations were made with $\Sigma \sigma^*$ for secondary and tertiary amines. The amines included in the correlations are not indicated other than that they have minimum steric No direct comparison between the ρ -values for the pK_a values of substituted ammonium ions with σ^* conrequirements. Furthermore, there are no values of correlation coefficient, standard deviation, or other measure of degree of correlation reported. We have therefore studied the correlation of these several sets of substituted ammonium ions with σ_{I} , σ_{m} , and σ_{p} in order to provide a check on our method of investigating substituent effects, since these sets would be expected to give best correlation with σ_I . The p-values for these sets are required for purposes of comparison with those of the amidinium, guanidinium, and nitroguanidine sets. Only substituents which do not show large resonance effects or are-electron donor by resonance have been included in these sets. The results show best correlation with σ_I in all the cases studied. The ρ -values for all of those sets in water at *25'* are about the same magnitude. Although *p* decreases steadily as N-methyl groups are introduced, the change is probably too small to be significant. As ρ for the substituted diethylammonium ions is approximately equal to *p* for substituted

(9) H K Hall Jr , *J Am. Chem.* **Soc** , **79, 6441 (1957)**

TABLE IV

T. **G.** Bonner and J. C. Lockhart, *J. Chem. Soc.,* **3858 (1958).** J. H. Bryden, L. **A.** Burk**^e**V. M. Clark, *Proc.* Ref. **12.** * IX predominates; hardt, and E. W. Hughes, *ibid.*, 9, 573 (1956). *Chem. SOC.,* **129 (1964).** *f* D. Prevorsek, *J. chim. phys.,* **840 (1958);** *J. Phys. Chem.,* **66, 769 (1962).** X is also found.

ammonium ions, it seems unlikely that the changes in ρ due to the introduction of N-methyl groups are real.

Discussion

Site of Ionizable Proton.^{---The} application of the Hammett equation to sets capable of prototropic tautomerism was first studied by Jaffé.¹⁰ Kabachnik¹¹ and his group have investigated several systems capable of exhibiting this phenomenon. Sets **2** and **3** are both capable of exhibiting tautomerism, which may be presented as follows.

$$
\begin{array}{cccc}\n\begin{array}{c}\n\text{NH} \\
\downarrow \\
\text{I} & \text{I} \\
\end{array} \\
\text{I} & \text{I} & \text{I} \\
\end{array}
$$

In carrying out the correlations it has been assumed that, when Y is an electron acceptor, the tautomer X will predominate as the result of loss of the N-1 proton. When Y is an electron donor, tautomer IX is considered predominant. On this basis, compounds with $Y =$ alkyl were excluded from set 3. Physical evidence in support of these assumptions has been reported by several authors and is summarized in Table IV. To this physical evidence may be added the following arguments.

(1) The ρ -value for the substituted guanidinium ions (set **3)** is very much larger than that for the substituted N-phenylamidinium ions (set **2),** and is in fact comparable with the ρ -values obtained for substituted ammonium ions (sets $5-9$). The magnitude of ρ is a function of the quantity correlated, the conditions under which it is measured, the structure of the set, and its molecular geometry. In comparing sets *2* and **3** the only variable is the molecular geometry. The variation of ρ with molecular geometry is given by eq. 2.

$$
\rho_{\rm G} = \frac{r_{\rm G}^{0^2} \cos \theta_{\rm G} \rho_{\rm G}^{0}}{r_{\rm G}^{2} \cos \theta_{\rm G}^{0}} \tag{2}
$$

We may write the set under consideration in the form XGY where X is the substituent, Y the reaction site, and G some group to which they are both attached. Similarly, we may consider some reference set XG^0Y .

Then in general r and θ are defined in XI. For acidbase equilibria, *r* represents the distance between the midpoint of the X-G bond and the ionizable proton, θ the angle made by this distance with the X-G bond dipole.

The comparison between the ρ -values of substituted ammonium ions and those of sets **2** and **3** is not so well justified. Furthermore, correlation of pK_a values of substituted phenylimines (XII) (PhXC=NH) with σ_m results in a ρ -value of about 19. Nevertheless, it does not seem possible to account for the large difference in p between sets **2** and 3 except in terms of the difference in *r* and *8* between the two sets.

(2) The best correlation of the pK_a values of substituted ammonium ions is obtained with the σ_I constants. Set 3 also gives best correlation with σ_1 . If ionization in set 3 were to occur at K-3 rather than **N-1,** then set 3 would constitute a subset of set 1; this would require that the relationship

$$
\sigma_m \cdot x_{\rm NH} = m \sigma_{\rm I, X} + c \tag{3}
$$

be fulfilled. Actually the equation

$$
\sigma_{m\text{-}XNH} = m\sigma_{m\text{-}X} + c \tag{4}
$$

gives best results. At this point we may also note that, although Koike¹² has reported on the basis of ultraviolet data that phenylguanidine has the structure X, he finds for the ionization of 4-substituted phenylguanidines in water, a ρ -value of 2.30 (compare ρ for substituted anilines = **2.767).** Ionization at N-3 should probably gave a ρ -value less than 1.

The ionization of the 3-nitroguanidines (set **4)** may also show tautomerism. Here again we have assumed that, when X is an electron acceptor, XIV is predomi-

$$
X-MH-C=MNO2\n
$$
\xrightarrow{\begin{subarray}{c} 1\\ \text{X-HH-C=NNO_2} \\ \text{XIII} \end{subarray}} X-MH-C=(3)NNO_2 \xleftarrow{\begin{subarray}{c} 2\\ \text{X-HH-C=3} \\ \text{X-HH}_{2} \end{subarray}} N_{1}N_{2}
$$
\n
$$
X-\bar{N}-C=NNO_2
$$
$$

⁽¹⁰⁾ H. H. Jaffé, *J. Am. Chem. Soc.*, 77, 4445 (1955); H. H. Jaffé and G. 0. Doak, *ibid.,* **77, 4441 (1955).**

⁽¹¹⁾ M. I. Kabachnik, T. **A.** Mastrukova. **A.** E. Shipov, andT. **A.** Melentyeva, *Tetrahedron,* **0,** 10 **(1900).**

⁽¹²⁾ H. Koike, *Nippon Kauahu Zasehi,* **88, 917 (1902); Chem.** *Abetr.,* **68, 13301e (1903).**

nant, whereas, when X is an electron donor, XI11 is the predominant tautomer. On the basis of this assumption, compounds with $X = Me$, PhCH₂, and PhCH₂CH₂ were excluded from the set. These assumptions are more difficult to justify as no physical evidence is available. They seem reasonable in view of the previous discussion. Furthermore, the second argument of the previous discussion is applicable here, as again decidedly best correlation is obtained with the σ_1 constants. We therefore consider that in set **4** the ionizable proton is situated at **S-1.**

Electrical Effects in C-Substituted Amidinium Ions. $-$ It has previously been shown that *trans*-vinylene sets are best correlated by the σ_p constants.¹³ The amidinium ions may be considered to be vinylene sets in which the reaction site is the nitrogen bearing the transferable proton. Thus the amidine set is analogous to the vinylene in the same sense that pyridine is analogous to benzene. The question then arises as to why the best results are obtained with σ_m constants rather than σ_p . In the course of another investigation¹⁴ we have observed that, although the" normal" electrical effect of ortho substituents is proportional to that of para substituents

$$
\sigma_o = m \sigma_p + c \tag{5}
$$

in ortho substituted pyridines and quinolines, an "abnormal" electrical effect is observed.

$$
\sigma_o = m\sigma_1 + c \text{ or } \sigma_o = m\sigma_m + c \tag{6}
$$

We believe that the amidinium ions represent an analogous situation. The geometry of the amidinium ions shows a strong resemblance to that of the 2-substituted pyridinium or quinolinium ions. Thus the explanation we have proposed for the "abnormal" ortho effect may be applied also to this unexpected electrical effect in amidinium ions. This explanation presumed the existence of a short-range localized electrostatic effect which we believe to be the classical inductive effect. The total electrical effect of a substituent may be represented as

$$
\sigma_T = \lambda \sigma_I + \delta \sigma_R \tag{7}
$$

where σ_1 is a constant characteristic of the localized effect and σ_R is a constant characteristic of the delocalized effect, λ and δ being the coefficients which determine the contribution of these effects to σ_T . Over more

(13) M. Cherton and H. Meislioh, *J. Am. Chem. SOC., 80,* **5940 (1958); J. Hine and W. C. Bailey.** *ibid.,* **81, 2075 (1959); J. Hine and** W. **C. Bailey,** *J. Ow. Chem.,* **16, 2098 (1961); P. B. D. de la Mare,** *J. Chem. Soc.,* **3823 (1960).**

(14) **M. Charton,** *J. Am. Chem. Soc.***, 86, 2033 (1964).**

then two bond lengths, we believe that the localized effect is largely a field effect. Over the short distance involved in the amidinium ions, the short-range localized (inductive) effect also makes a significant contribution, thus increasing the magnitude of λ and presumably leaving δ unaffected. This will result in a change in ϵ where

$$
\epsilon = \delta/\lambda \tag{8}
$$

As can be seen from the values of ϵ in Table V, a decrease in ϵ could lead to an electrical effect better represented by σ_m than by σ_n .

^{**a}** Ref. 14, unless otherwise noted. **b** M. Charton, unpublished</sup> results.

Electrical Effects in Substituted Ammonium Ions.- It seems significant that the ρ -values of the substituted ammonium ions are almost unaffected by the presence of N-alkyl groups. While the electrical effect of such groups would not be greatly different from that of hydrogen (σ_I for Me and Et is -0.05 , for H it is 0), the variation in size and shape on introduction of N-alkyl groups should change the effective dielectric constant of the ammonium ion. Thus, if the predominant component of the localized effect in these species was the field effect, some significant change in ρ might be expected. Using the Kirkwood-Westheimer equation,¹⁵ and assuming that the $N-H$ bond length, the $X-N$ bond lengths, and the XNH angle are about the same

$$
\log \frac{K_{\rm X}}{K_{\rm H}} = \frac{e_{\mu \rm X} \cos \theta}{2.303RT D_{\rm E} r^2} = \rho \sigma_{\rm X} \tag{9}
$$

for some N-alkyl set, while for the unsubstituted set

$$
\rho^0 \sigma_X = \frac{e\mu_X \cos \theta}{2.303RT D_E^0 r^2} \tag{10}
$$

and

$$
\rho = \frac{D_{\mathbf{E}}^0 \rho^0}{D_{\mathbf{E}}} \tag{11}
$$

The absence of such an important change in ρ can be explained in terms of the inductive effect as the major component of the localized effect in the substituted ammonium ions.

(15) J. G. Kirkwood and F. H. Westheimer, *J. Chem. Phye.,* **6,** *506,* **513 (1938).**